Problem Set 3

Ch153a - Winter 2023

Due: 20 January 2023

- 1. Construct a diagram illustrating the dependence of electrode potentials (vs. NHE) on pH (Pourbaix diagram) for the following redox couples:
 - a. $O_2 + e^- + H^+ \rightarrow HO_2^{\bullet}$
 - b. $HO_2^{\bullet} + e^- + H^+ \rightarrow H_2O_2$
 - c. $H_2O_2 + e^- + H^+ \rightarrow HO^{\bullet} + H_2O$
 - d. $HO^{\bullet} + e^{-} + H^{+} \rightarrow H_{2}O$
 - e. $O_2 + 2e^- + 2H^+ \rightarrow H_2O_2$
 - f. $H_2O_2 + 2e^- + 2H^+ \rightarrow 2H_2O$
 - g. $O_2 + 4e^- + 4H^+ \rightarrow 2H_2O$

In constructing your diagram, use the following standard potentials:

$$O_2 + e^- \rightarrow O_2^{\bullet-}$$

$$E^{\circ} = -0.35 \text{ V } vs. \text{ NHE}$$

$$HO_2^{\bullet} + e^- \rightarrow HO_2^-$$

$$HO_2^{\bullet} + e^- \rightarrow HO_2^ E^{\circ} = 0.76 \text{ V vs. NHE}$$

$$H_2O_2 + e^- + H^+ \rightarrow HO^{\bullet} + H_2O$$
 $E^{\circ} = 0.80 \text{ V } vs. \text{ NHE}$

$$E^{\circ} = 0.80 \text{ V } vs. \text{ NHE}$$

$$HO^{\bullet} + e^{-} + H^{+} \rightarrow H_{2}O$$

$$E^{\circ} = 2.72 \text{ V } vs. \text{ NHE}$$

and the following pK_a values:

$$HO_2^{\bullet} \rightarrow O_2^{\bullet-} + H^+$$

$$pK_a = 4.8$$

$$H_2O_2 \rightarrow HO_2^- + H^+$$

$$pK_a = 11.62$$

$$HO^{\bullet} \rightarrow O^{\bullet-} + H^{+}$$

$$pK_a = 11.7$$

$$H_2O \rightarrow HO^- + H^+$$

$$pK_a = 14.0$$

The standard state for potentials is 25 °C, concentrations of 1 molal (1 m), partial gas pressures of 100 kPa, and the activity of water is taken to be unity. For the purposes of your diagram, assume the following conditions:

$$pO_2 = 100 \text{ kPa}$$

$$[HO_2^{\bullet}] + [O_2^{\bullet-}] = 1 m$$

$$[H_2O_2] + [HO_2^-] = 1 m$$

$$[HO^{\bullet}] + [O^{\bullet-}] = 1 m$$

Your plot should span the range from pH 0 to pH 14.

- 2. Using the data from your Pourbaix diagram give the electrode potentials for the redox couples a-q at the following pH values:
 - a. pH 0
- b. pH 7 c. pH 14
- 3. Using the data from your Pourbaix diagram determine the standard free energy change for the following reaction:

$$2HO^{\bullet} \Longrightarrow H_2O_2$$

4. It should be clear from your Pourbaix diagram that the electrode potential for the fourelectron, four-proton oxidation of water is substantially lower than those for some of the steps in the sequential one-electron oxidation of water to dioxygen. The stepwise oxidation of water, then, requires large overpotentials; these overpotentials can be reduced if the intermediates in the water oxidation sequence are bound to metal complexes as illustrated below. Define the potential for redox reaction q from question 1 (pH 7, 25 °C) to be equal to that for the oxygen evolving reaction (E_{OER}).

$$E_{d} \uparrow \downarrow \qquad \qquad \swarrow E_{OER}$$

$$2HO^{\bullet} + 2H^{+} + 2e^{-} + M(OH_{2})_{2}^{n+} \qquad \stackrel{K_{1}}{\longleftrightarrow} \qquad 2H^{+} + 2e^{-} + M(OH)_{2}^{n+} + 2H_{2}O$$

$$\Delta G_{1}^{\circ} \uparrow \downarrow \qquad \qquad \downarrow \uparrow \Delta G^{\circ} = 0$$

$$H_{2}O_{2} + 2H^{+} + 2e^{-} + M(OH_{2})_{2}^{n+} \qquad \stackrel{K_{2}}{\longleftrightarrow} \qquad 3H^{+} + 2e^{-} + M(OH_{2})(O_{2}H)^{(n-1)+} + H_{2}O$$

$$E_{b} \uparrow \downarrow \qquad \qquad \downarrow \uparrow E_{OER}$$

$$HO_{2}^{\bullet} + 3H^{+} + 3e^{-} + M(OH_{2})_{2}^{n+} \qquad \stackrel{K_{3}}{\longleftrightarrow} \qquad 3H^{+} + 3e^{-} + M(OH_{2})(O_{2}H)^{n+} + H_{2}O$$

$$E_{a} \uparrow \downarrow \qquad \qquad \downarrow \uparrow E_{OER}$$

$$O_{2} + 4H^{+} + 4e^{-} + M(OH_{2})_{2}^{n+} \qquad \stackrel{K_{4}}{\longleftrightarrow} \qquad 4H^{+} + 4e^{-} + M(OH_{2})(O_{2})^{n+} + H_{2}O$$

Use the data from your Pourbaix diagram and the answer from question 3 (ΔG_1°) to estimate values for the equilibrium constants for binding to a generic metal center $(M(OH_2)_2^{n+})$ of the intermediates in the water oxidation sequence, i.e., K_1 , K_2 , K_3 , and K_4 .